

بإستخدام الإستنتاج الرياضي اثبت أن:

$$1^3 + 2^3 + 3^3 + \dots + n^3 = \left(\frac{1}{2} n(n+1) \right)^2 .1$$

$$1(1!) + 2(2!) + 3(3!) + \dots + n(n!) = (n+1)! - 1 .2$$

$$1^2 - 2^2 + 3^3 - 4^2 + \dots - (2n)^2 = -n(2n+1) .3$$

$$1^2 - 2^2 + 3^3 - 4^2 + \dots + (2n+1)^2 = (n+1)(2n+1) .4$$

$$\sum_{r=1}^n \frac{1}{(3r-2)(3r+1)} = \frac{n}{3n+1} .5$$

$$\frac{8}{3*5} - \frac{12}{5*7} + \frac{16}{7*9} - \dots \text{to } n \text{ terms} = \frac{1}{3} + (-1)^{n-1} \frac{1}{2n+3} .6$$

$$\frac{1^2}{1*3} + \frac{2^2}{3*5} + \frac{3^2}{5*7} + \dots \text{to } n \text{ terms} = \frac{n(n+1)}{2(2n+1)} .7$$

$$\begin{bmatrix} -2 & 9 \\ -1 & 4 \end{bmatrix}^n = \begin{bmatrix} 1-3n & 9n \\ -n & 1+3n \end{bmatrix} .8$$

$$\begin{bmatrix} \cos x & -\sin x \\ \sin x & \cos x \end{bmatrix}^n = \begin{bmatrix} \cos nx & -\sin nx \\ \sin nx & \cos nx \end{bmatrix} .9$$

$$n \geq 2 \text{ لقيم } \frac{1}{\sqrt{1}} + \frac{1}{\sqrt{2}} + \dots + \frac{1}{\sqrt{n}} > \sqrt{n} .10$$

$$n > 5 \text{ لقيم } n! > n^3 .11$$